

1. Was passiert, wenn $a < 0$ und $b > 0$ ist? (Skizzieren Sie!)

$$\int_a^b f(x) dx = \int_a^0 f(x) dx + \int_0^b f(x) dx = F(0) - F(a) + F(b) - F(0) = F(b) - F(a)$$

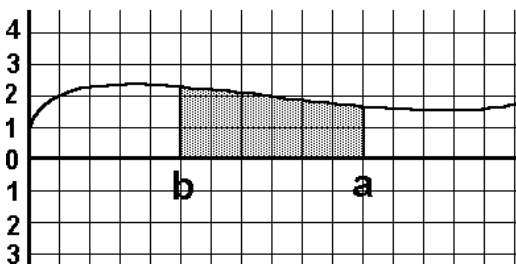
2. Was passiert, wenn $a < 0$ und $b < 0$ ist? (Skizzieren Sie!)

$$\int_a^b f(x) dx = \int_a^0 f(x) dx - \int_b^0 f(x) dx = F(0) - F(a) - [F(0) - F(b)] = F(0) - F(a) - F(0) + F(b) = F(b) - F(a)$$

Zusammenfassung:

Ist $a < b$, so gilt: $\int_a^b f(x) dx = F(b) - F(a)$

3. Was passiert, wenn $a > b$ ist?



$$\int_a^b f(x) dx = \int_0^a f(x) dx - \int_0^b f(x) dx = F(a) - F(0) - [F(b) - F(0)] = F(a) - F(0) - F(b) + F(0) = F(a) - F(b) = - [F(b) - F(a)] = - \int_a^b f(x) dx$$

4. Für $a < c < b$ gilt:

$$\begin{aligned} \int_a^c f(x) dx + \int_c^b f(x) dx \\ = F(c) - F(a) + F(b) - F(c) = F(b) - F(a) \\ = \int_a^b f(x) dx \end{aligned}$$

5. Was passiert, wenn $f(x) < 0$ ist?

Ist $f(x) \leq 0$ im Intervall $[a; b]$, so gilt:

$$\int_a^b f(x) dx = - \int_a^b f(x) dx \text{ oder } \left| \int_a^b f(x) dx \right|$$

6. Summenregel der Integration:

$$\int_a^b f(x) + g(x) dx = [F(x) + G(x)]_a^b = [F(b) + G(b)] - [F(a) + G(a)] = F(b) - F(a) + G(b) - G(a) =$$

$$\int_a^b f(x) dx + \int_a^b g(x) dx$$

7. Faktorregel der Integration:

$$\int_a^b r \cdot f(x) dx = r \cdot F(b) - r \cdot F(a) = r [F(b) - F(a)] = r \cdot \int_a^b f(x) dx$$